

**Table 1.1**

$h$ (cm)	$t$ (s)			
	$d = 1.5$ mm	$d = 2.0$ mm	$d = 3.0$ mm	$d = 5.0$ mm
30.0	73.0	41.2	18.4	6.80
10.0	43.5	23.7	10.5	3.90
4.0	26.7	15.0	6.80	2.20
1.0	13.5	7.20	3.70	1.50

**III. DATA**

1. Use the data in Table 1.1 to fill in Table 1.2

**Table 1.2**

$d$ (mm)	$t$ (s)			
	$h = 1.0$ cm	$h = 4.0$ cm	$h = 10.0$ cm	$h = 30.0$ cm
1.5	13.5	26.7	43.5	73.0
2.0	7.20	15.0	23.7	41.2
3.0	3.70	6.80	10.5	18.4
5.0	1.50	2.20	3.90	6.80

2. For  $h = 30$  cm, use Tables 1.1 and 1.2 and fill in Table 1.3.

**Table 1.3**

$t$ (s)	$d$ (mm)	$1/d^2$ (mm <sup>-2</sup> )
73.0	1.5	0.4
41.2	2.0	0.25
18.4	3.0	0.1
6.80	5.0	0.04

3. For  $d = 2.0$  mm, fill in Table 1.4 below:

**Table 1.4**

$t$ (s)	$h$ (cm)	$\text{Log}_{10}(t)$	$\text{Log}_{10}(h)$
41.2	30.0	1.6	1.47
23.7	10.0	1.37	1
15.0	4.0	1.17	0.6
7.20	1.0	0.85	0

## V. ANALYSIS OF DATA

### 1. Plot your results.

- Using a scale that utilizes at least  $2/3$  of the sheet of graph paper, plot on the *same graph paper* (using the same axes) the function  $t(h)$  (i.e.,  $t$  vs.  $h$ ) for each diameter ( $d$ ) used. Connect the data points from each case with a smooth curve, and label each curve with the corresponding  $d$ .
- Similarly, on a second sheet of graph paper, plot the function  $d(t)$  (i.e.,  $d$  vs.  $t$ ) for each value of the height ( $h$ ). Connect the points corresponding to each value of  $h$  with a smooth curve and label each curve with the appropriate value of  $h$ .
- Plot  $t$  versus  $1/d^2$  for  $h = 30$  cm.
- Plot  $\text{Log}_{10}(t)$  versus  $\text{Log}_{10}(h)$  for  $d = 2$  mm.

### 2. Use your graphs to answer the following questions:

- a. From your graph of  $(h)$  versus  $(t)$  for  $d = 1.5$  mm, extrapolate the curve toward the origin. Does it pass through it? Would you expect it to do so? Explain.

Yes it will pass through origin, I expect it. There's no water in the container so there's no time to measure.

- b. What type of relationship (direct or inverse) do you see between the time  $t$  and diameter  $d$  for a fixed value of  $h$ ? Why?

Inverse because when the time increase the diameter lessens.

- c. From the graph of  $t$  versus  $1/d^2$ , determine the *empirical relationship* between time  $t$  and hole diameter  $d$  for  $h = 30$  cm.

$$y = mx + b$$

$$t = \frac{m}{d^2}$$

$$t = \frac{m}{d^2} = 149$$

d. From the previous relation, calculate the time needed to empty the container if the diameter of the hole is 4 mm.

$$t = \frac{m}{(4)^2} \quad t = \frac{0.5}{4^2}$$

see part i

e. From the  $\text{Log}_{10}(t)$  versus  $\text{Log}_{10}(h)$  graph, find the empirical relationship between the time  $t$  and height  $h$  for  $d = 2$  mm.

$$y = mx + b$$

$$\text{Log}(t) = \text{Slope} \times \text{Log}(h) + b$$

$$t = (h^m)(10^b)$$

f. From the previous relation, obtained in the previous step, calculate the time needed to empty the container if the height of water was 25 cm.

$$y = mx + b$$

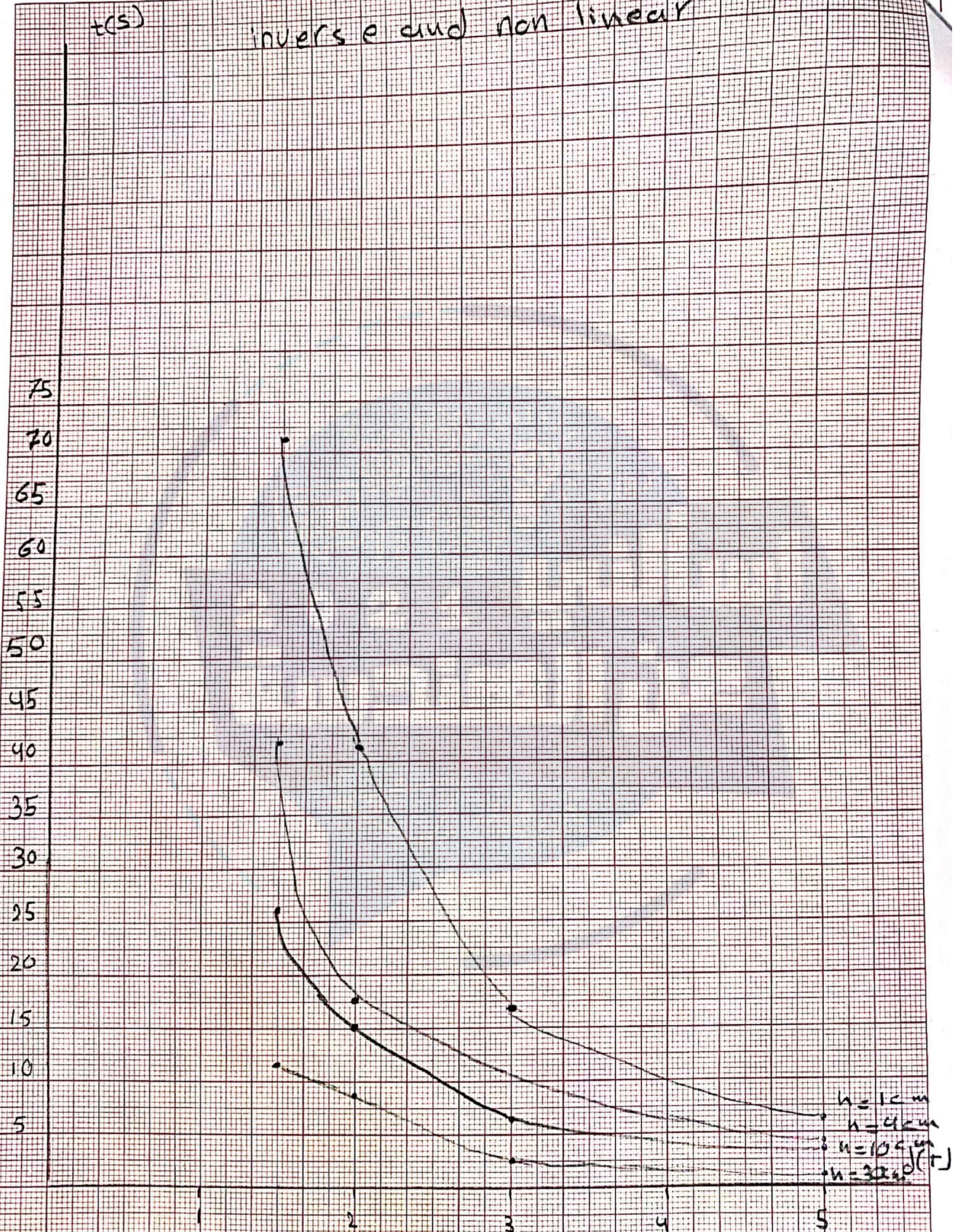
$$\text{Log}_{10} t = m \text{Log}_{10} h + b \Rightarrow t = 10^b h^m$$

part i

g. What is meant by an empirical relationship?

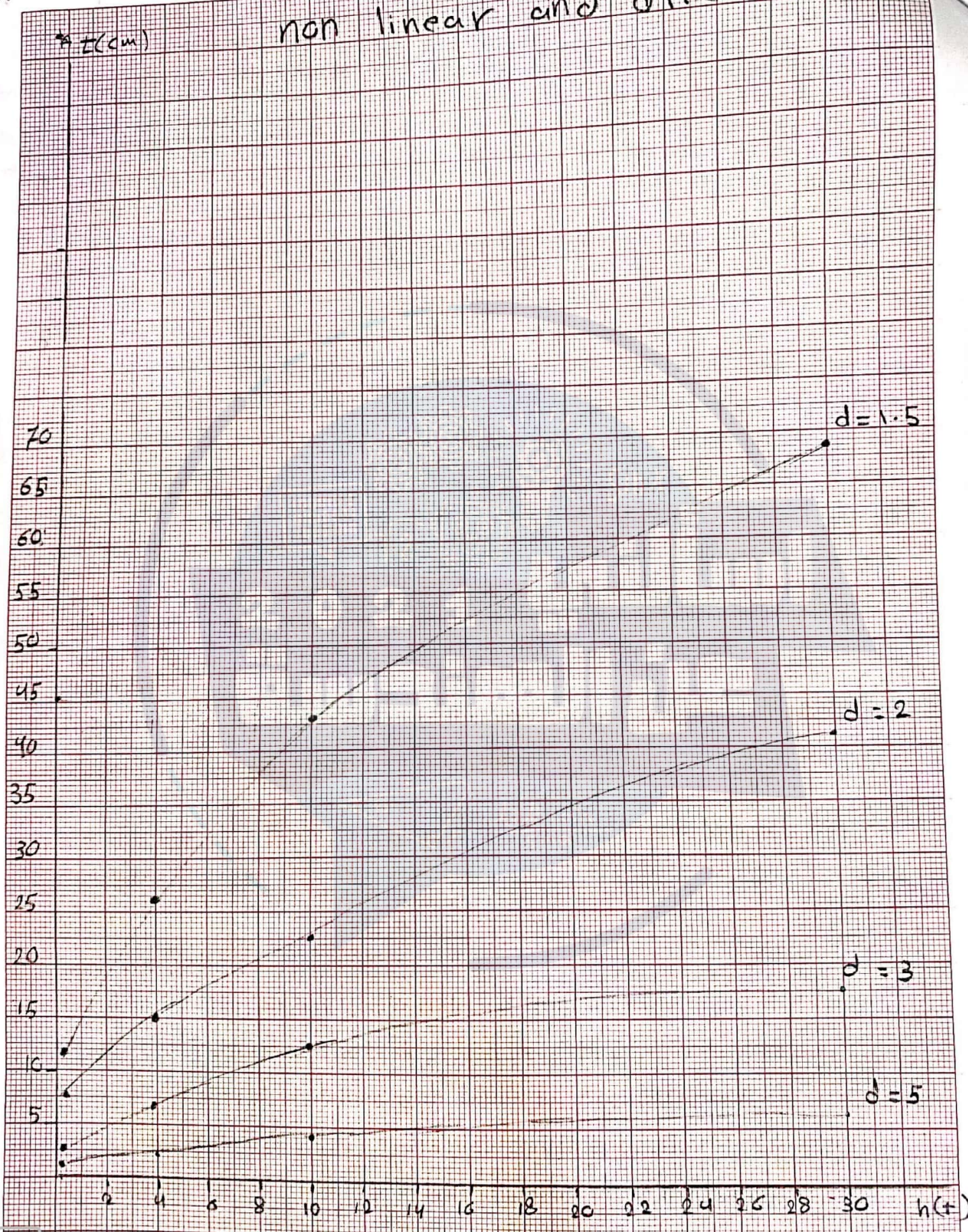
# $t(s)$ versus $d(t)$

inverse and non linear



$t(\text{cm})$  versus  $h(\tau)$

non linear and direct



$t(s)$  versus  $1/d^2$

$t(s)$

$$\text{slope} = \frac{\Delta y}{\Delta x} =$$

$$\frac{54 - 37}{0.3 - 0.2} = 170 \text{ s/mm}^{-2}$$

80  
75  
70  
65  
60  
55  
50  
45  
40  
35  
30  
25  
20  
15  
10  
5

0.1 0.2 0.3 0.4

$1/d^2$

( $\text{mm}^{-2}$ )

# Log(t) versus log(n)

log t

$$\text{slop} = \frac{\Delta y}{\Delta x} =$$

(0.4, 1)

(1, 1.3)

$$\frac{1.3 - 1}{1 - 0.4} =$$

= 0.5

