

Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  
 $g = 9.8 \text{ m/s}^2$

If the force between two charges has magnitude 3.36 N when the charges are separated by 8.0 mm, the magnitude of the force (in N) between these two charges when separated by 16 mm is

- a. 5.97
- b. 2.15
- c. 0.84
- d. 13.44
- e. 1.49

Clear my choice



Q1:

$$F_1 = k \frac{q_1 q_2}{(8 \times 10^{-3})^2} = 3.36 \text{ N} \rightarrow (1)$$

$$F_2 = k \frac{q_1 q_2}{(16 \times 10^{-3})^2} \rightarrow (2) \quad k = \frac{1}{4\pi\epsilon_0}$$

$$\text{eqn } 2 \div 1 : \frac{F_2}{3.36} = \frac{(8 \times 10^{-3})^2}{(16 \times 10^{-3})^2}$$

$$\frac{F_2}{3.36} = \frac{1}{4} \quad \boxed{F_2 = 0.84 \text{ N}}$$

\(\therefore\) the answer is C

9.8 m/s<sup>2</sup>

If  $a = 60$  cm,  $b = 80$  cm,  $Q = -2.0$  nC, and  $q = 1.5$  nC, what is the magnitude of the electric field (in N/C) at point P?



- a. 47
- b. 56
- c. 68
- d. 80
- e. 92

Clear my choice

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$$Q2: E_1 = k \frac{q_1}{r_1^2} = \frac{9 \times 10^9 + 2 \times 10^{-9}}{(0.8)^2} = 28.13 \text{ N/C}$$

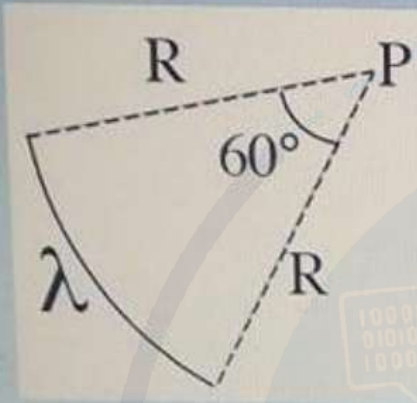
$$E_2 = k \frac{q_2}{r_2^2} = \frac{9 \times 10^9 + 1.5 \times 10^{-9}}{(0.6)^2} = 37.5 \text{ N/C}$$

$$|E| = \sqrt{E_1^2 + E_2^2} \\ = \sqrt{(28.13)^2 + (37.5)^2} = 46.88 \text{ N/C}$$

∴ the answer is  $\boxed{46.88}$

9.8 m/s<sup>2</sup>

A charge of uniform density  $\lambda = 2 \text{ nC/m}$  is distributed along the circular arc shown in the figure. Taking the electric potential to be zero at infinity, the electric potential (in V) at point  $P$  is



- a. 11.2
- b. 18.9
- c. 28.3
- d. 37.7

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$$Q3: \theta = \frac{60 + 2\pi}{360} = \frac{I}{3} \text{ rad}$$

$$\lambda = 2 \times 10^{-9} \text{ C}$$

$$V = k \lambda \theta = 9 \times 10^9 \times 2 \times 10^{-9} \times \frac{I}{3}$$

$$= 18.85 \text{ V} \quad \text{the answer is } \boxed{b}$$

$$e = 1.6 \times 10^{-19} \text{ C}; m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}; m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg};$$

$$g = 9.8 \text{ m/s}^2$$

A proton accelerates from rest in a uniform electric field of 500 N/C. At one later moment, its speed is  $1.30 \times 10^6 \text{ m/s}$ . Over what time interval (in  $\mu\text{s}$ ) does the proton reach this speed?

- a. 27
- b. 48
- c. 69
- d. 90
- e. 13

Clear my choice

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$$\text{proton} = 1.6 \times 10^{-19}$$

$$E = 500 \text{ N/C}$$

$$v_1 = 0 \text{ m/s}$$

$$v_2 = 1.3 \times 10^6 \text{ m/s}$$

$t = ??$

$$1) F = q \cdot E = am$$

$$= \frac{1.6 \times 10^{-19} \times 500}{1.67 \times 10^{-27}} = \frac{1.67 \times 10^{-27} \times a}{1.67 \times 10^{-27}}$$

$$a = 4.79 \times 10^{10}$$

$$2) v_2 = v_1 + at$$

$$1.3 \times 10^6 = 0 + 4.79 \times 10^{10} \times t$$

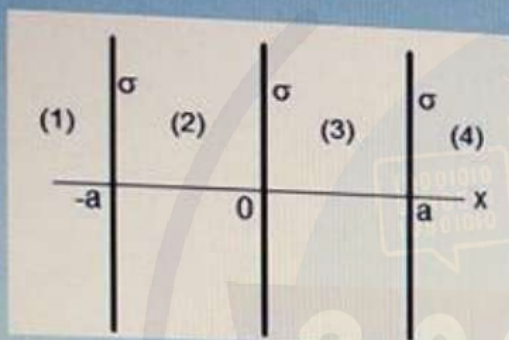
$$\boxed{t = 27} \quad \text{the answer is } \boxed{a}$$



### Useful Constants

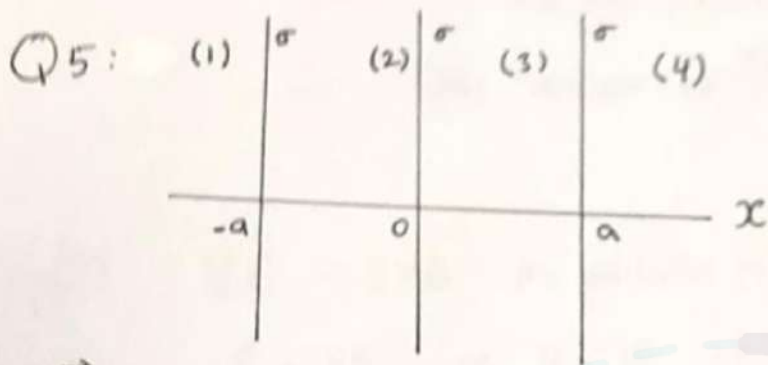
$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$   
 $g = 9.8 \text{ m/s}^2$

Three infinite, nonconducting parallel sheets carry equal uniform charge densities  $\sigma$  as shown in the figure. The electric field in region (3) is



- a.  $(3\sigma/2\epsilon_0)$  in the negative x-direction
- b.  $(\sigma/2\epsilon_0)$  in the negative x-direction
- c. Zero
- d.  $(\sigma/2\epsilon_0)$  in the positive x-direction
- e.  $(3\sigma/2\epsilon_0)$  in the positive x-direction

Clear my choice



→  $\vec{E}$  due to infinite non conducting parallel sheets is given by:

$$E = \frac{\sigma}{2\epsilon_0}$$

→  $\vec{E}$  due to the sheet (a) at  $x = -a$  is given by:

$$E_A = \frac{\sigma}{2\epsilon_0} \text{ in positive } x\text{-direction}$$

→ the same for the sheet B at  $x = 0$ :

$$E_B = \frac{\sigma}{2\epsilon_0} \text{ in positive } x\text{-direction}$$

→ for the sheet C at  $x = a$ :

$$E_C = -\frac{\sigma}{2\epsilon_0} \text{ in negative } x\text{-direction}$$

\* The electric field in region (3) is:

$$E = E_A + E_B + E_C$$

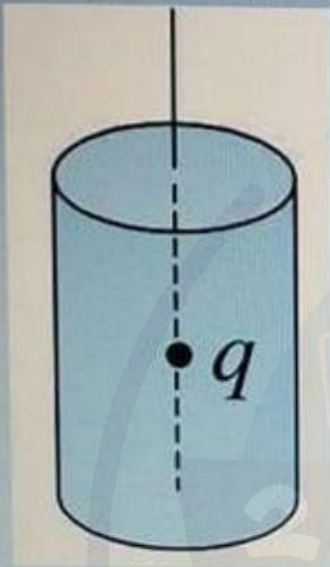
$$= \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0} - \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{2\epsilon_0}$$

$$E = \frac{\sigma}{2\epsilon_0} \text{ in the positive } x\text{-direction}$$

the answer is d

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

If a point charge is located at the center of a cylinder and the electric flux leaving one end of the cylinder is 15% of the total flux leaving the cylinder, the portion of the flux that leaves the curved surface of the cylinder is



- a. 80%
- b. 70%
- c. 85%

$$\text{Total flux} = \frac{q}{\epsilon_0} = \phi$$

~~$\phi_1 = 15\%$~~   $\phi_1 = 15\%$  of  $\phi$  flux passing through flat surface 1  
 $\phi_2 = 15\%$  of  $\phi$  " " " " " " 2

$\phi_3 =$  Remaining flux passing through curved surface 3

$$= (100 - 30)\% \text{ of } \phi$$

$$\phi_3 = 70\% \text{ of } \phi$$

**B**



A parallel plate capacitor stores a charge of 50 mC when a potential difference of 100 V exists between its plates. The charge (in mC) stored in a spherical capacitor with twice the capacitance of the parallel-plate capacitor when a potential difference of 200 V is applied to it is:

Select one:

- 150
- 200
- 25
- 100
- 50

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Q7:  $q = CV$

So:  $C = \frac{q}{V} = \frac{50 \times 10^{-3}}{100} = \frac{10^{-3}}{2} \text{ F}$

for spherical capacitor:

$$q = 2CV$$
$$= 2 \times \frac{10^{-3}}{2} \times 200$$

$= 200 \text{ ms}$  the answer is **[b]**

proton moves in a circle due to the force of a uniform magnetic field of 0.835 T. If the magnitude of the linear momentum of the proton is  $1.336 \times 10^{-19} \text{ kg.m.s}^{-1}$ , then the radius (in m) of the circle is:

Select one:

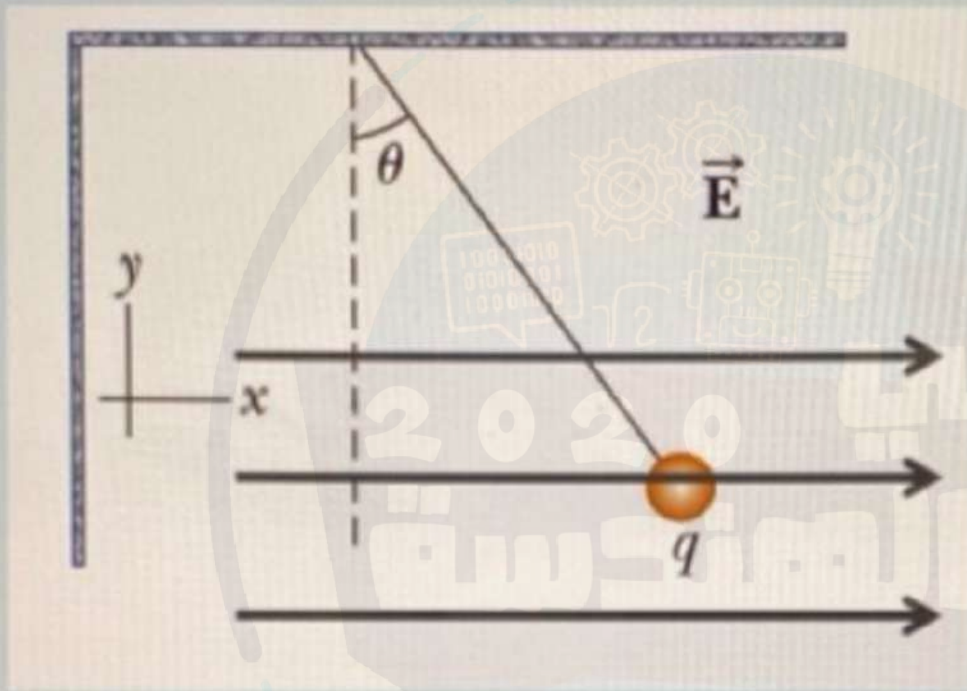
- 1.198
- 0.697
- 1.0
- 1.785
- 0.835

$$Q_8: r = \frac{mv}{qB} = \frac{1.336 \times 10^{-19}}{1.6 \times 10^{-19} \times 0.835}$$

$r = 1.0$  the answer is [C]



As shown in the figure, a small ball with charge  $q$  and a mass 3.80 grams is attached to a horizontal ceiling by a wire of length 130.0cm. When an electric field,  $E$ , of magnitude 3085 N/C is applied, the ball swings away from the vertical axis with an angle  $\theta = 42^\circ$ , therefore,  $q$  (in  $\mu\text{C}$ ) is:



Select one:

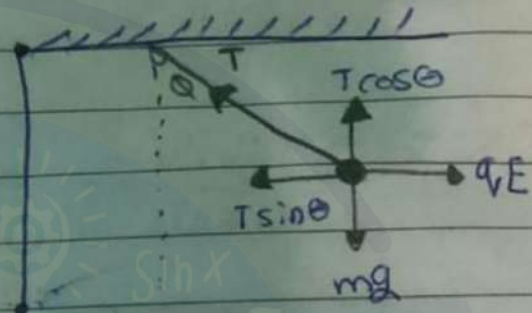
- 3.01
- 8.97
- 10.87
- 6.66
- 8.08

$$m = 3.80 \text{ g} = 3.8 \times 10^{-3} \text{ kg}$$

$$L = 130 \text{ cm}$$

$$E = 3085 \text{ N/C}$$

$$\theta = 42$$



$$T \cos \theta = mg \quad (1)$$

$$T \sin \theta = qE \quad (2)$$

$$\frac{(2)}{(1)} \rightarrow \frac{T \sin \theta}{T \cos \theta} = \frac{qE}{mg} \Rightarrow \tan \theta = \frac{qE}{mg}$$

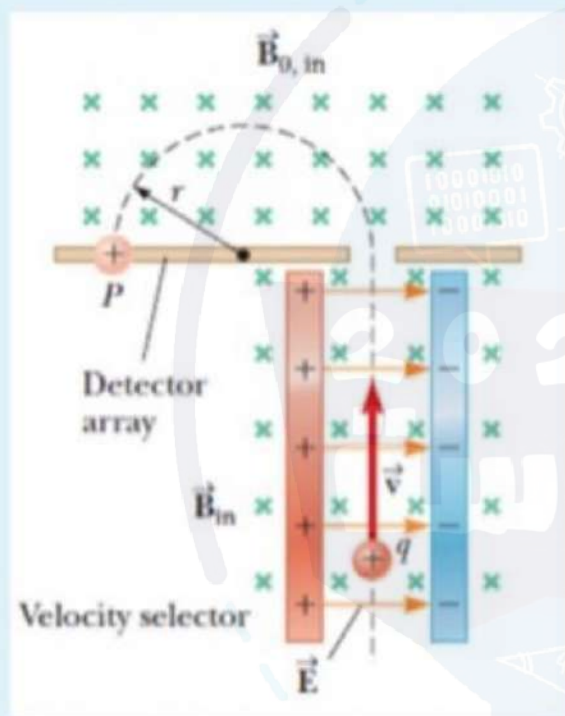
$$q = \frac{mg \cdot \tan \theta}{E}$$

$$= \frac{3.8 \times 10^{-3} \times 9.8 \times \tan(42)}{3085} = 10.8690 \times 10^{-6} \text{ C}$$
$$= 10.8690 \text{ MC}$$

$$\approx 10.87 \text{ MC}$$

The answer is C

In the mass spectrometer shown, a positive charge  $q$  of mass  $m$  is sent first through a velocity selector with a velocity  $v$  in the presence of a magnetic field  $\mathbf{B}$  and an electric field  $\mathbf{E}$ . Upon entering the second magnetic field  $\mathbf{B}_0$ , the charge  $q$  moves in a semicircle of radius  $r$  before striking a detector array at  $P$ , as shown. The radius  $r$  can be expressed as:



Select one:

- $mBB_0/vE$
- $mE/qBB_0$
- $E/mBB_0$

Q10:  $qE = qvB$  as particle is going straight

$$E = vB \Rightarrow v = \frac{E}{B} = \frac{E}{B \sin \theta}$$

After that it is going in a circular motion

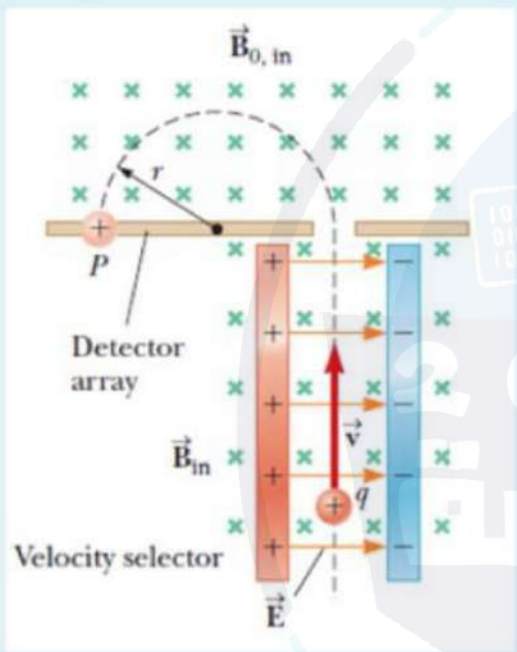
$$r = \frac{mv}{qB_0}$$

$$\text{and } v = \frac{E}{B \sin \theta}$$

$$r = \frac{mE}{qBB_0}$$

the answer is  $\boxed{B}$

In the mass spectrometer shown, a positive charge  $q$  of mass  $m$  is sent first through a velocity selector with a velocity  $v$  in the presence of a magnetic field  $B$  and an electric field  $E$ . Upon entering the second magnetic field  $B_0$ , the charge  $q$  moves in a semicircle of radius  $r$  before striking a detector array at  $P$ , as shown. The strength of the second field  $B_0$  can be expressed as:



- Select one:
- $mv/EB$
  - $vE/mrB$
  - $mE/qrB$
  - $rmB/vE$
  - $qE/vB$

Q11:  $F_{\text{magnetic}} = F_{\text{electric}}$

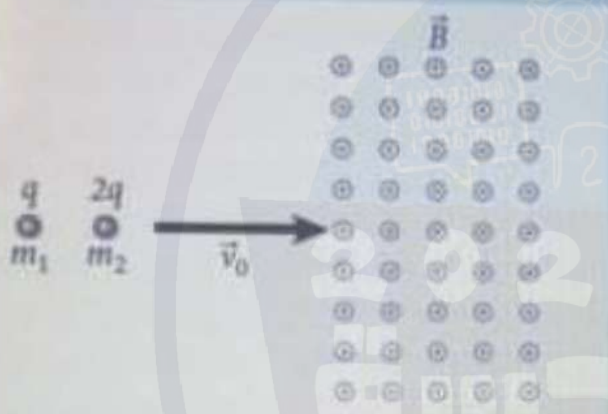
$$Eq = Bvq \Rightarrow v = \frac{E}{B}$$

$F_{\text{magnetic}} = F_{\text{centrifugal}}$

$$B_0 vq = \frac{mv^2}{r} \Rightarrow B_0 q = \frac{m}{r} v$$

$$B_0 = \frac{m}{qr} \left( \frac{E}{B} \right) = \frac{mE}{qrB} \quad \text{the answer is } \boxed{C}$$

The two particles shown in the figure enter the magnetic field at the same point, with the same velocity. Accordingly, in the magnetic field, they move in circles with radii  $r_1 = r$  and  $r_2 = 2r$ . The ratio of their masses,  $[m_1/m_2]$ , is:



Select one:

- 4
- 1
- 2
- 1/2
- 1/4

$$r_1 = \frac{m_1 v}{q_1 B}$$

$$r_1 \rightarrow \frac{m_1 \times v}{q_1 B}$$

$$r_2 = \frac{m_2 \times v}{2q_2 \times B}$$

$$\frac{r_1}{r_2} \rightarrow \frac{\frac{m_1 v}{q_1 B}}{\frac{m_2 v}{2q_2 B}}$$

$$\frac{r_1}{r_2} \rightarrow$$

$$\frac{r}{2r} \rightarrow \frac{2m_1}{m_2}$$

$$\frac{m_1}{m_2} = \frac{1}{4}$$

D



Two identical conducting spheres (#1 and #2) carry charges  $Q$  and  $3Q$  respectively. They are separated by a distance  $r$  much larger than their diameters. Another identical conducting sphere (#3) is uncharged. Sphere #3 is first touched to #1, then to #2, and finally removed. As a result, the Coulomb force between #1 and #2, which was originally  $F$ , becomes:

Select one:

- $9F$
- $7F/8$
- $3F/14$
- $7F/24$
- $8F/15$



$q_1 =$  charge on sphere 1 =  $Q$   
 $q_2 =$  charge on sphere 2 =  $3Q$   
 $q_3 =$  charge on sphere 3 =  $0$

$$F = \frac{kQ \times 3Q}{r^2}$$

\* when 3 touches 1, then new charge on 1 is  $Q/2$  and 3 is also  $Q/2$ .  $\rightarrow$  Now 3 touches 2  $\rightarrow$  then new charge on 2 is

$$\frac{3Q + \frac{Q}{2}}{2} = \frac{7Q}{4}$$

Final charge on 1 is  $Q/2$  / and 2 is  $7Q/4$

$$F' = k \times \frac{Q}{2} \times \frac{7Q}{4} = \frac{k \times \frac{Q}{2} \times \frac{7Q}{4}}{r^2} \times \frac{3}{3} = \boxed{\frac{7F}{24}} \quad \boxed{r}$$

An infinite conducting cylinder has a radius of 12.0 mm. If the magnitude of the electric field 16.0 mm from the axis of the cylinder is 55 N/C, what is the charge density distributed over the surface of the cylinder (in nC/m<sup>2</sup>)?

$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2\cdot\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$$

Select one:

- 4.87
- 0.89
- 0.70
- 0.65
- 0.07

[Clear my choice](#)

$$R = 12 \text{ mm}, \gamma = 16 \quad E = 55 \text{ N/c} \quad h = ?$$

$$E = \frac{2k\lambda}{r}$$

$$55 = \frac{2 \times 9 \times 10^9 \times h}{16 \times 10^{-3}}$$

$$h = 4.889 \times 10^{-11} \text{ c/m}$$

[A]

A thin wire of length  $L$  has a uniform charge density  $\lambda$ . The wire is bent into a semicircle with its center at the origin. The magnitude of the electric field at the center of the semicircle is  $1.5 \times 10^4$  (in N/C). If  $\lambda = 5.6 \times 10^{-8}$  C/m, what is the value of  $L$  (in cm)?

$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2\cdot\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$$

Select one:

- 21.1
- 0.8
- 18.1
- 4.4
- 7.0

$$\pi r = L \quad \text{or} \quad r = L/\pi$$

$$E = \frac{2k\lambda}{r} = \frac{2k\lambda}{L/\pi}$$

$$L = \frac{2\pi k\lambda}{E} = \frac{2\pi \times 9 \times 10^9 \times 5.6 \times 10^{-9}}{1.5 \times 10^4} = 0.211 \text{ m} = 21.1 \text{ cm}$$

**A**

A total charge of 10.0 nC is distributed uniformly through an insulating sphere with a radius of 14.00 mm. The total electric flux (in  $\text{N}\cdot\text{m}^2/\text{C}$ ) through a concentric sphere with a radius of 7.00 mm is:

$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$$

Select one:

- 684.6
- 2101.4
- 749.4
- 141.2
- 34.7

The volume charge density  $\rho = \frac{Q}{V}$        $Q = 10 \text{ nC} = 10 \times 10^{-9} \text{ C}$   
 $Q = 14 \text{ mV} = 14 \times 10^{-3} \text{ m}$

$$\rho = \frac{Q}{\frac{4}{3}\pi R^3} \quad \rho = \frac{90 \times 10^{-9}}{(4\pi)(2.744 \times 10^{-2})^3} \quad \frac{\text{C}}{\text{m}^3}$$

$$\rho = 8.70016 \times 10^{-4} \text{ C/m}^3$$

• according to Gauss's law

$$\Phi = \frac{q}{\epsilon_0}$$

$$\epsilon_0 = 8.85 \times 10^{-12}$$

$$q = (\rho) \left( \frac{4}{3} \pi r^3 \right)$$

$$8.70016 \times 10^{-4} \left( \frac{\text{C}}{\text{m}^3} \right) \times \frac{4}{3} \pi \times (7 \times 10^{-3} \text{ m})^3$$

$$q = 1.25 \times 10^{-9} \text{ C}$$

$$\text{now } \phi = \frac{q}{\epsilon_0} = \frac{1.25 \times 10^{-9} \text{ C}}{8.85 \times 10^{-12} \text{ C/Vm}^2}$$

$$\phi = 141.243 \frac{\text{Vm}^2}{\text{C}} \quad \boxed{D}$$



A total charge of 25.0 nC is distributed uniformly through an insulating sphere with a radius of 18.00 mm. The total electric flux (in  $\text{N m}^2/\text{C}$ ) through a concentric sphere with a radius of 9.00 mm is:

$$K = 9 \times 10^9 \text{ N.m}^2.\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2.\text{N}^{-1}.\text{m}^{-2}$$

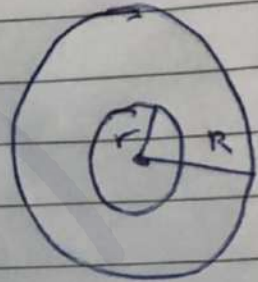
Select one:

- 7840.7
- 2040.8
- 12.2
- 4.2
- 353.1

$$Q = 25 \text{ nC} = 25 \times 10^{-9} \text{ C}$$

$$R = 18 \text{ mm}$$

$$\rho = \frac{Q}{\text{volume}} = \frac{Q}{\frac{4}{3} \pi R^3}$$



$$r = 9 \text{ mm}$$

$$Q_v = \rho \left( \frac{4}{3} \pi r^3 \right)$$

$$\text{volume of sphere} = \frac{4}{3} \pi r^3$$

$$Q = \frac{Q}{\frac{4}{3} \pi R^3} \times \frac{4}{3} \pi r^3 = \frac{Q r^3}{R^3} = \frac{25 \times 10^{-9} \times (9)^3}{(18)^3}$$

$$Q = 3.125 \times 10^{-9} \text{ (C)}$$

$$\text{now } \phi = \frac{Q}{\epsilon_0} = \frac{3.125 \times 10^{-9}}{8.85 \times 10^{-12}} = \boxed{353.11 \text{ Nm}^2/\text{C}}$$
  
$$\boxed{E}$$

The point charge  $q_1$  ( $+4 \mu\text{C}$ ) is located at  $x_1 = -5.7\text{m}$ , and the point charge  $q_2$  ( $+9 \mu\text{C}$ ) is located at  $x_2 = +14.1\text{m}$ , as shown in the figure. The net electric force on a point charge  $q_3$  ( $+5 \mu\text{C}$ ) is zero at the  $x$ -coordinate (in m):



$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2\cdot\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$$

Select one:

- +11.0
- 3.1
- +2.2
- 1.2
- +15.7

Force on  $q_3$  due to  $q_1$  and  $q_2$

$$\vec{F}_3 = \vec{F}_{13} + \vec{F}_{23}$$

$q_1 = 5 \text{ mC}$       $q_2 = 9 \text{ mC}$   
 $x_1 = 5.7$       $x_2 = 14.1 \text{ m}$

$d$  between  $q_1$  and  $q_2 = 19.8 \text{ m}$

$d$  between  $q_1$  and  $q_3 = x$

$d$  between  $q_2$  and  $q_3 = d - x$

$$F_{13} = \frac{(4 \times 10^{-6} \text{ C})(5 \times 10^{-6} \text{ C})}{4\pi \epsilon_0 x^2} = \frac{0.18}{x^2} \quad (\text{along } +x \text{-axis})$$

$$F_{23} = \frac{q_2 q_3}{4\pi \epsilon_0 (d-x)^2} = \frac{0.405}{(d-x)^2} \quad (\text{along } -x \text{ axis})$$

net force = 0

$$F_{13} = F_{23}$$

$$\frac{0.18}{x^2} = \frac{0.405}{(d-x)^2} \Rightarrow 0.18(d^2 + x^2 - 2dx)$$

$$= 0.405x^2$$

$$\Rightarrow 0.225x^2 + 7.128x - 70.57 = 0 \quad x = 7.92 \text{ m or } -39.6 \text{ m}$$

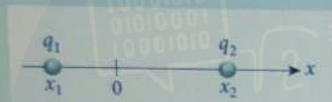
$$q_3 = 7.92 \text{ m} - 5.7 \text{ m} = \boxed{+2.2 \text{ m}} \quad \text{C} \quad \text{impossible}$$

A conducting sphere of radius  $R$  carries a net positive charge  $Q$ , uniformly distributed over the surface of the sphere. Assuming that the electric potential is zero at an infinite distance, what is the electric potential at a distance  $r = R/8$  from the center of the sphere?

Select one:

- $8kQ/R$
- $kQ/8R$
- $kQ/R$
- zero
- $64kQ/R$

The point charge  $q_1$  ( $+5 \mu\text{C}$ ) is located at  $x_1 = -3.6\text{m}$ , and the point charge  $q_2$  ( $+7 \mu\text{C}$ ) is located at  $x_2$  as shown in the figure. The net electric force on a point charge  $q_3$  ( $-1 \mu\text{C}$ ) is zero at the  $x$ -coordinate  $+4.6\text{m}$ . The value of  $x_2$  (in m) is:



$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2\cdot\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$$

Select one:

- +11.0
- +8.2
- +14.3
- +0.7
- +3.6



$$\frac{b^2 - c^2}{\sin a}$$

$$q_1 = 5 \mu\text{C} = 5 \times 10^{-6}$$

$$q_2 = 7 \mu\text{C} = 7 \times 10^{-6}$$

$$q_3 = -1 \mu\text{C} = 1 \times 10^{-6} \text{ C}$$

$$x_1 = -3.6 \quad x_2 = 4.6 \quad x_2 = ?$$

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

Net in  $q_3$  is zero

$$\frac{1}{4\pi\epsilon_0} \frac{q_1 q_3}{(x_1 + x)^2} = \frac{1}{4\pi\epsilon_0} \frac{q_2 q_3}{(x_2 - x)^2}$$

$$\frac{5 \times 10^{-6}}{(-3.6 + 4.6)^2} = \frac{7 \times 10^{-6}}{(x_2 - 4.6)^2} = 94.136$$

$$(x_2 - 4.6)^2 = 9.7$$

$$x_2 = 9.7 + 4.6$$

$$x_2 = 14.3 \text{ C}$$

A thin wire of length  $L$  has a uniform charge density  $\lambda$ . The wire is bent into a semicircle with its center at the origin. The magnitude of the electric field at the center of the semicircle is  $2 \times 10^{+4}$  (in N/C). If  $\lambda = 6.1 \times 10^{-9}$  C/m, what is the value of  $L$  (in cm)?

$$K = 9 \times 10^{+9} \text{ N.m}^2.\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2.\text{N}^{-1}.\text{m}^{-2}$$

Select one:

- 9.0
- 17.2
- 3.4
- 5.4
- 14.2



$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



$$E = 2 \times 10^4 \text{ N/C}$$

$$f = 6.1 \times 10^{-6} \text{ C/m}$$

$$E = \frac{2kf}{R}$$

$$R = \frac{2kf}{E}$$

$$= \frac{2 \times 9 \times 10^9 \times 6.1 \times 10^{-6}}{2 \times 10^4}$$

$$R = 5.49 \text{ m}$$

the length of wire  $= \pi R = \pi \times 5.49$

$$L = 17.25 \text{ m}$$

**(B)**

The potential along the  $y$ -axis is given by  $V(y) = -8y + 3y^2$  in units of V. At what value(s) of  $y$  (in m) is (are) the electric field equal to zero?

Select one:

- +4/3
- 0 or +4
- 0 or +8/3
- +8/3
- 0

$$V(y) = -8y + 3y^2$$

$$E = \frac{-dV}{dy} = \frac{-d}{dy} (-8y + 3y^2)$$

$$\rightarrow E = -(-8 + 6y)$$

$$E = 0 \quad -(-8 + 6y) = 0$$

$$6y = 8$$

$$y = \frac{4}{3}$$

A

A thin wire of length  $L$  has a uniform charge density  $\lambda$ . The wire is bent into a semicircle with its center at the origin. The magnitude of the electric field at the center of the semicircle is  $3 \times 10^4$  (in N/C). If  $L = 10.55$  cm, what is the value of  $\lambda$  (in C/m)?

$$K = 9 \times 10^9 \text{ N.m}^2.\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2.\text{N}^{-1}.\text{m}^{-2}$$

Select one:

- $7.4 \times 10^{-6}$
- $4.4 \times 10^{-7}$
- $8.2 \times 10^{-7}$
- $5.6 \times 10^{-8}$
- $8.2 \times 10^{-8}$

An infinite conducting cylinder has a radius of 7.0 cm. If the magnitude of the electric field 11.0 cm from the axis of the cylinder is 23 N/C, what is the charge density distributed over the surface of the cylinder (in nC/m<sup>2</sup>)?

$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2\cdot\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$$

Select one:

- 0.06
- 0.47
- 0.89
- 6.04
- 0.32

A proton ( $m = 1.67 \times 10^{-27}$  kg) is placed a distance  $y$  above a long, horizontal wire of linear charge density  $\lambda$ . The proton is then released from rest. Determine the magnitude of the initial acceleration of the proton (in  $\text{m/s}^2$ ). Take  $\lambda = 2.8 \times 10^{-12}$  C/m and  $y = 70$  cm.

$$K = 9 \times 10^9 \text{ N}\cdot\text{m}^2\cdot\text{C}^{-2}, \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$$

Select one:

- $1.9 \times 10^7$
- $6.9 \times 10^6$
- $8.8 \times 10^6$
- $4.4 \times 10^7$
- $7.4 \times 10^6$

Particle A (of mass  $m$  and charge  $q$ ) and particle B (of mass  $4m$  and charge  $2q$ ) are each accelerated from rest through the same potential difference of  $4000\text{ V}$ . Which one of the following statements regarding their resulting speeds is TRUE:

Select one:

- Particle A has twice the speed of particle B.
- The speed of particle A is  $\sqrt{2}$  times the speed of particle B.
- Particle A has the same speed as particle B.
- Particle A has half the speed of particle B.
- The speed of particle B is  $\sqrt{2}$  times the speed of particle A.

For A : Electrostatic Potential Energy = EPE =  $qV$

$$\text{Kinetic Energy} = \frac{1}{2} mV_a^2$$

$$EPE = K.E$$

$$qV = \frac{1}{2} mV_a^2 \quad V \equiv \text{potential}$$

$$V_a = \sqrt{\frac{2qV}{m}}$$

For B: EPE =  $2qV$

$$K.E = \frac{1}{2} (4m)V_B^2$$

$$EPE = K.E$$

$$2qV = \frac{1}{2} \cdot 4mV_B^2$$

$$V_B = \sqrt{\frac{qV}{m}}$$

$$\therefore V_a = \sqrt{2} V_B$$

the answer is **D**



## Useful Constants

$$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2; \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2;$$

$$e = 1.6 \times 10^{-19} \text{ C}; m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}; m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg};$$

$$g = 9.8 \text{ m/s}^2$$

The magnitude of the acceleration (in  $\text{m/s}^2$ ) of a proton in a uniform electric field of magnitude  $3 \times 10^4 \text{ N/C}$  is

- a.  $1.9 \times 10^{12}$
- b.  $3.5 \times 10^{12}$
- c.  $2.9 \times 10^{12}$
- d.  $4.8 \times 10^{12}$
- e.  $6.7 \times 10^{12}$

### Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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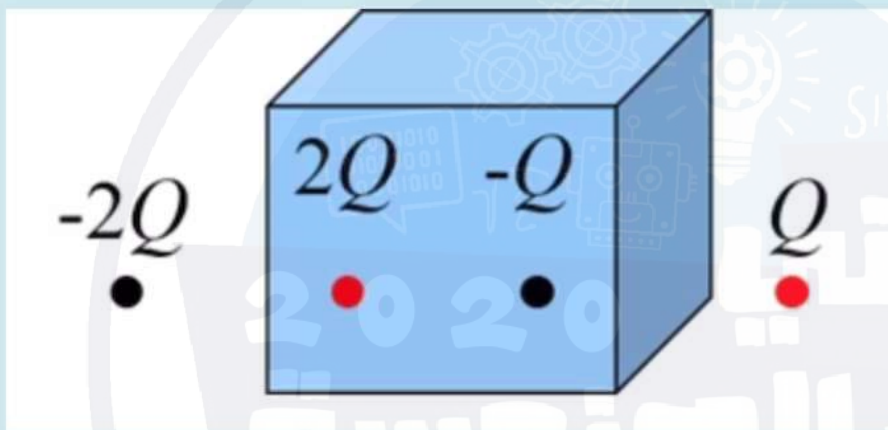
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The magnitude of the electric potential (in V) at a point that is 3.0 m away from a 1.5 nC point charge is

- a. 3.0
- b. 4.5
- c. 5.2
- d. 6.0
- e. 9.6

Next page

The figure shows a closed cubical surface with the charges  $2Q$  and  $-Q$  inside the cube and the charges  $-2Q$  and  $Q$  outside the cube. If  $Q = 4 \text{ nC}$  the net electric flux (in  $\text{N}\cdot\text{m}^2/\text{C}$ ) through the surface of the cube is



- a. 282
- b. 0
- c. 452
- d. 734
- e. 565

### Useful constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N.m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N.m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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The surface charge density on the surface of a conducting sphere is  $4 \text{ nC/m}^2$ . The magnitude of the electric field at the surface of the sphere (in  $\text{N/C}$ ) is:

- a. 226
- b. 452
- c. 678
- d. 930
- e. 1130

## Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N.m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N.m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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Over a certain region of space, the electric potential is  $V = 5x - 3x^2y + 2yz^2$  volts. The magnitude of the electric field (in N/C) at the point  $P$  that has coordinates  $(1, 0, 1)$  m is

- a. 5.1
- b. 5.6
- c. 10.7
- d. 15.8
- e. 18.6

## Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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A charged nonconducting ball with a mass of 0.0300 kg and a total charge of +50.0  $\mu\text{C}$  is hung from a ceiling by a light nonconducting string of length 15.0 cm. The ball is subjected to a uniform, downward electric field of magnitude 2000 N/C. The tension (in N) in the string is:

- a. 0.394
- b. 0.194
- c. 0
- d. 0.294
- e. 0.100

## Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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There is a  $1.5 \times 10^{-3} \text{ N}$  electric force in the negative y-direction on a  $-3.00 \text{ nC}$  point charge at the point with coordinates  $(-1.00 \text{ m}, 0.00 \text{ m}, 0.00 \text{ m})$ . The electric field (in N/C) at this point is given by:

- a.  $5.0 \times 10^5$  in the positive y-direction
- b.  $5.0 \times 10^5$  in the negative y-direction
- c.  $5.0 \times 10^5$  in the positive x-direction
- d.  $5.0 \times 10^5$  in the negative x-direction
- e.  $1.5 \times 10^5$  in the positive y-direction

## Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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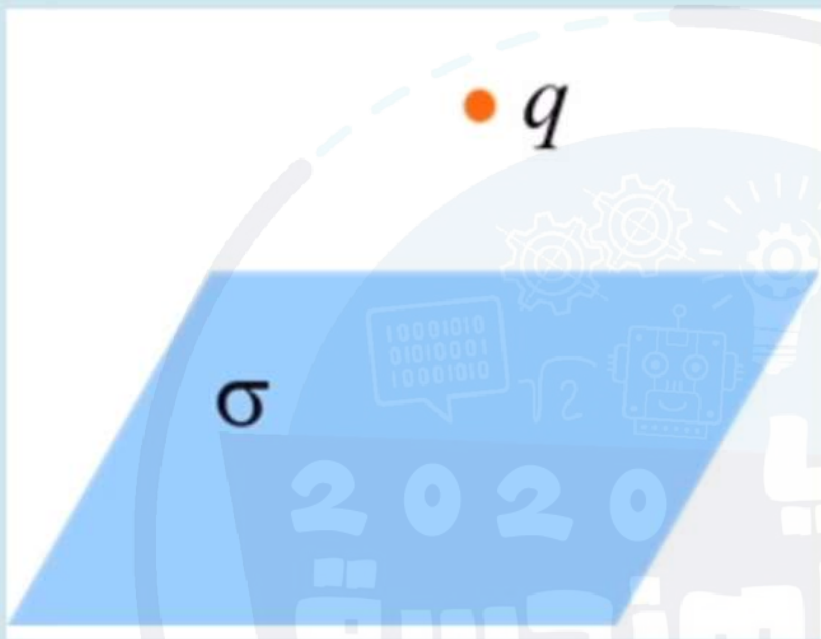
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A solid conducting sphere of radius  $R$  carries a net positive charge  $2Q$ . The electric potential  $V$  at a distance  $r = R/2$  from the center of the sphere is

- a.  $5k_e Q/R$
- b.  $4k_e Q/R$
- c.  $3k_e Q/R$
- d.  $2k_e Q/R$
- e.  $k_e Q/R$



A 10.0-g small plastic ball carries a net charge  $q = 0.70 \mu\text{C}$  and floats (تطفو) at rest above an infinite horizontal sheet of plastic that has a uniform surface charge density  $\sigma$  on its surface. The surface charge density  $\sigma$  (in  $\mu\text{C}/\text{m}^2$ ) on the plastic sheet is



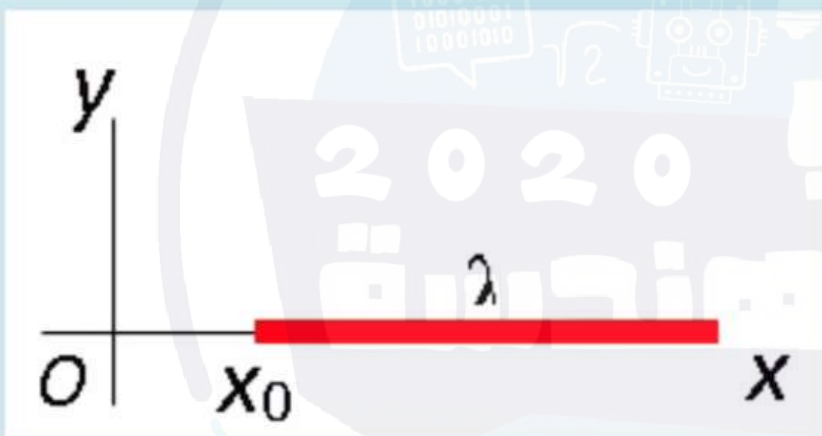
- a. -2.5
- b. 2.5
- c. -4.3
- d. 4.3
- e. 0.7

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$


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A line of charge lying along the  $x$ -axis starts at  $x=+x_0$  and extends to positive infinity. It has a nonuniform linear charge density  $\lambda = \lambda_0 x_0/x$ , where  $\lambda_0$  is a positive constant. The magnitude of the electric field at the origin  $O$  is



- a.  $4k_e\lambda_0$
- b.  $4k_e\lambda_0/x_0$
- c.  $2k_e\lambda_0/x_0$
- d.  $k_e\lambda_0/x_0$
- e.  $k_e\lambda_0/2x_0$

2. Charges  $q_1$  and  $q_2$  are on the  $x$  axis, with  $q_1$  at  $x = a$  and  $q_2$  at  $x = 2a$ . For the net force on a another charge at the origin to be zero  $q_1$  and  $q_2$  must be related by  $q_2 =$ : \* 

(3 Points)

- $2q_1$
- $4q_1$
- $-2q_1$
- $-4q_1$
- $-q_1/4$

Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

Consider an insulating solid sphere of radius  $R = 0.1 \text{ m}$  and uniform volume charge density  $\rho = 2.4 \times 10^{-4} \text{ C/m}^3$ . The magnitude of the electric field at distance  $r = 0.15 \text{ m}$  from the center of the sphere (in N/C) is

- a.  $4.0 \times 10^5$
- b.  $2.3 \times 10^5$
- c.  $1.8 \times 10^5$
- d.  $1.4 \times 10^5$
- e.  $1.0 \times 10^5$

### Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$


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A proton released from rest in a region of a uniform electric field undergoes a displacement through a potential difference of  $-150 \text{ V}$ . The change in its kinetic energy (in eV) is

- a.  $-150$
- b.  $150$

5. 10 C of charge are placed on a spherical conducting shell. A  $-3\text{-C}$  point charge is placed at the center of the cavity. The net charge in coulombs on the inner surface of the shell is: \*  
(3 Points)

- 7
- 3
- 0
- +3
- +7

8. Three charges lie on the x axis:  $1 \times 10^{-8} \text{ C}$  at  $x = 1 \text{ cm}$ ,  $2 \times 10^{-8} \text{ C}$  at  $x = 2 \text{ cm}$ , and  $3 \times 10^{-8} \text{ C}$  at  $x = 3 \text{ cm}$ . The potential energy (in J) of this arrangement, relative to the potential energy for infinite separation, is: \*   
(3 Points)

- $7.9 \times 10^{-2}$
- $8.5 \times 10^{-4}$
- $1.7 \times 10^{-3}$
- 0.16
- 0

6. Charge  $Q$  is distributed uniformly throughout a spherical insulating shell. The net electric flux in  $\text{N} \times \text{m}^2/\text{C}$  through the outer surface of the shell is: \*  (3 Points)

- 0
- $Q/\epsilon$
- $2Q/\epsilon$
- $Q/4\epsilon$
- $Q/2\pi\epsilon$

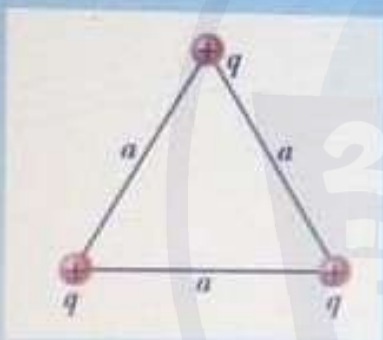


7. A conducting sphere of radius 0.01 m has a charge of  $1.0 \times 10^{-9}$  C deposited on it. The magnitude of the electric field in N/C just outside the surface of the sphere is: \* (3 Points)

- 0
- 450
- 900
- 4500
- 90000

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

Three particles with equal positive charges  $q = 10.0 \mu\text{C}$  are at the corners of an equilateral triangle of side  $a = 3.0 \text{ cm}$  as shown in the figure. What is the electric potential energy (in J) of the system of three particles?



- a. 270
- b. 90

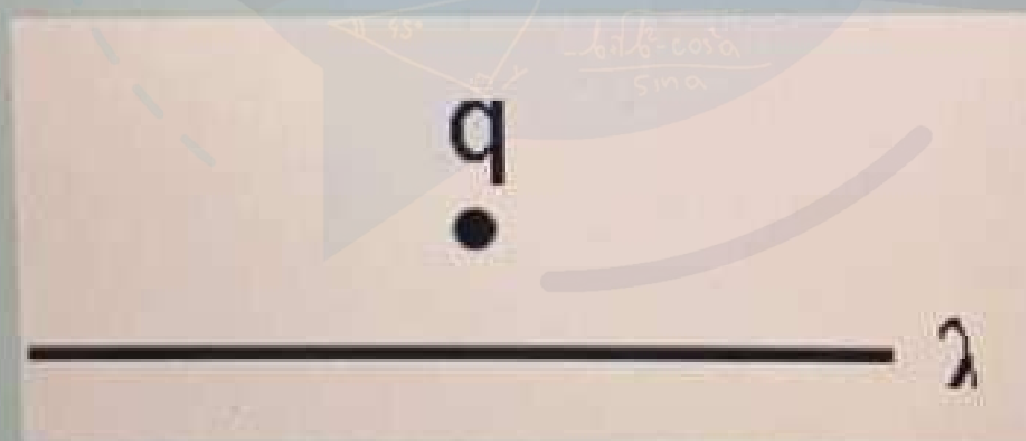
### Useful Constants

$$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2; \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2; e = 1.6 \times 10^{-19} \text{ C}; m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}; m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}; g = 9.8 \text{ m/s}^2$$

If a charge of  $30 \mu\text{C}$  is located  $5.0 \text{ cm}$  from a charge of  $6.5 \mu\text{C}$ , the electric potential energy (in J) of this arrangement is

- a. 35
- b. 14
- c. 21
- d. 28

A 2.0-g small plastic ball carries a net positive charge at (تطفو) of  $5.0 \mu\text{C}$  and floats rest 1.0 mm directly above an infinitely long horizontal line of positive charge having a uniform charge per unit length  $\lambda$  as shown. The magnitude of  $\lambda$  (in nC/m) is



Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

A closed cube of edge length  $L = 0.5 \text{ m}$  is resting within a horizontal electric field of magnitude  $E = 3.2 \times 10^2 \text{ N/C}$  as shown in the figure. The electric flux through the left face (in  $\text{N}\cdot\text{m}^2/\text{C}$ ) is:



- a. 0
- b. -145
- c. 145
- d. -80
- e. 80


Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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If a charge of  $12 \mu\text{C}$  is located  $5.0 \text{ cm}$  from a charge of  $6.5 \mu\text{C}$ , the electric potential energy (in J) of this arrangement is

- a. 35
- b. 14
- c. 21
- d. 28
- e. 7

9. The potential difference between two points is 100 V. If 2 C is transported from one of these points to the other, the magnitude of the work done is: \*   
(3 Points)

- 200 J
- 100 J
- 50 J
- 100 V
- 2 J

### Useful Constants

$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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If the electric flux through a closed surface is  $565 \text{ N}\cdot\text{m}^2/\text{C}$ , the net charge (in nC) inside the closed surface is:

- a. 0
- b. 5
- c. 4
- d. 2.5
- e. 6.5

Clear my choice

Next page

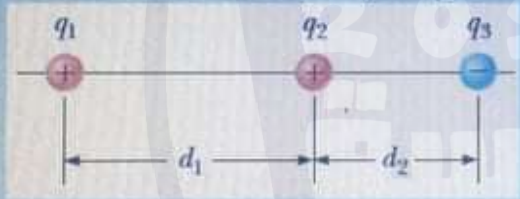


### Useful Constants


$k_e = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ;  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg}$ ;  $m_{\text{proton}} = 1.67 \times 10^{-27} \text{ kg}$ ;  $g = 9.8 \text{ m/s}^2$

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Three point charges lie along a straight line as shown in the figure below, where  $q_1 = 6.36 \mu\text{C}$ ,  $q_2 = 1.49 \mu\text{C}$ , and  $q_3 = -2.16 \mu\text{C}$ . The separation distances are  $d_1 = 3.00 \text{ cm}$  and  $d_2 = 2.00 \text{ cm}$ . The net electric force (in N) on  $q_2$  is




- a. 167.2 to the right
- b. 334.4 to the right
- c. 0
- d. 167.2 to the left

3. The magnitude of the force (in N) of a 400-N/C electric field on a 0.02-C point charge is: \*   
(3 Points)


- 8
- 0.08
- 8000
- $2 \times 10^{11}$
- $8 \times 10^{-5}$

1. Two small charged objects repel each other with a force  $F$  when separated by a distance  $d$ . If the charge on each object is reduced to one-fourth of its original value and the distance between them is reduced to  $d/2$  the force becomes: \*   
(3 Points)

- $F/16$
- $F/8$
- $F/4$
- $F/2$
- $F$

10. A 5-cm radius conducting sphere is charged until the electric field just outside its surface is 2000 V/m. The electric potential of the sphere (in V), relative to the potential far away, is: \* 

- 0
- 5
- 100
- $4 \times 10^4$
- $8 \times 10^5$

4. A spherical shell has an inner radius of 3.7 cm and an outer radius of 4.5 cm. If charge is distributed uniformly throughout the shell with a volume density of  $6.1 \times 10^{-4}$  C/m<sup>3</sup> the total charge (in C) is: \*   
(3 Points)

- $1.0 \times 10^{-7}$
- $1.3 \times 10^{-7}$
- $2.0 \times 10^{-7}$
- $2.3 \times 10^{-7}$
- $4.0 \times 10^{-7}$

①  $ma = Eq$

$(1.67 \times 10^{-27}) a = (3 \times 10^{-4}) (1.6 \times 10^{-19})$

$a = 2.87 \times 10^{12} \approx 2.9 \times 10^{12} \text{ m/s}^2$

Ⓒ

②  $V = \frac{kq_1 q_2}{r} = \frac{(9 \times 10^9)(1.5 \times 10^{-9})}{3} = 4.5 \text{ V}$

Ⓑ

③  $\phi = \frac{\sum q_{in}}{\epsilon_0} = \frac{2Q + (-Q)}{\epsilon_0}$   
 $= \frac{Q}{\epsilon_0} = \frac{4 \times 10^9}{8.85 \times 10^{-12}} = 451.97$

$\approx 452$

Ⓒ

④  $E = \frac{\sigma}{\epsilon_0} = \frac{4 \times 10^9}{8.85 \times 10^{-12}} = 451.97$

$\approx 452$

Ⓑ

⑤  $v = 5x - 3x^2y + 2yz^2$

$E = -\frac{\partial v}{\partial r}$  at  $(1, 0, 1)$

$\vec{E} = -(5 - 6xy)\hat{i} - (-3x^2 + 2z^2)\hat{j} - (4yz)\hat{k}$

$= -(5)\hat{i} - (-3)\hat{j} - 0\hat{k}$

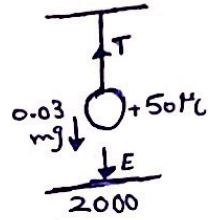
$\vec{E} = -5\hat{i} + 3\hat{j}$

$|\vec{E}| = \sqrt{(-5)^2 + (3)^2} = 5.99 \approx 5.1$

Ⓐ

\* ⑥  $m = 0.03 \quad q = +50 \times 10^{-6}$

$E = 2000 \quad g = 9.8$



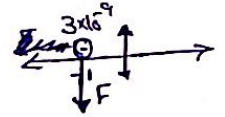
$T = mg + Eq$

$T = (0.03)(9.8) + (2000)(50 \times 10^{-6})$   
 $= 0.394$  Ⓐ

\* ⑦  $E = \frac{F}{q}$

$E = \frac{1.5 \times 10^{-3}}{3 \times 10^{-9}} = 5 \times 10^5 \text{ N/C}$

in the positive y-direction



Ⓐ

⑧  $r = R/2 < R$

$V = \frac{kq}{R}$

$V = \frac{2kQ}{R}$  Ⓐ

⑨  $E = \frac{\sigma}{2\epsilon_0}$

$E = \frac{F}{q} \quad F = mg$

$\frac{mg}{q} = \frac{\sigma}{2\epsilon_0} \Rightarrow \sigma = \frac{2mg\epsilon_0}{q}$

$\sigma = \frac{2(0.1 \times 10^{-3})(9.8)(8.85 \times 10^{-12})}{0.7 \times 10^{-6}} = 2.478 \times 10^{-6} \text{ C/m}^2$   
 $\approx 2.5 \times 10^{-6} \text{ C/m}^2 \approx 2.5 \mu\text{C/m}^2$

Ⓑ

\* ⑩

$E = \frac{k\lambda L}{D^2 + DL}$

$L = \infty$

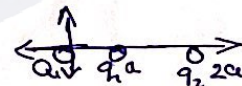
$L = \infty \Rightarrow E = \frac{k\lambda}{D}$

$D = x_0$

$\lambda = \frac{\lambda_0 x_0}{x}$

$E = \frac{k \lambda_0 x_0}{x_0 x} = \frac{k \lambda_0}{x}$  Ⓐ

Ⓐ



$F = 0 = \frac{kq_1 q_1}{x^2} = \frac{kq_1 q_2}{4x^2}$

$q_2 = 4q_1$

بما انه نقطة الاستراة خارج النقطتين لذا  
 كما يمكنه الاشارة

$q_2 = -4q_1$

Ⓐ

12\*  $r > R$

$$E = \frac{\rho R^2}{3\epsilon_0 r^2} = \frac{(2.4 \times 10^{-4})(0.10)^2}{3(8.85 \times 10^{-12})(0.15)^2}$$

$$= 4.017 \times 10^6 \approx 4 \times 10^6$$

(a) but there is something wrong

13\*  $\Delta KE = -\Delta U = -q \frac{\Delta V}{e} = -\frac{e \Delta V}{e} = -\Delta V$

= 150

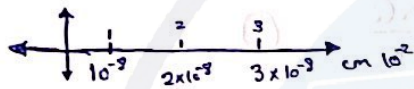
(b)

14

+3

(d)

15



$$U = \frac{kq_1q_2}{r_{12}} + \frac{kq_1q_3}{r_{13}} + \frac{kq_2q_3}{r_{23}}$$

$$= 8.55 \times 10^{-4} \approx 8.5 \times 10^{-4}$$

(b)

16

(b)  $\frac{Q}{\epsilon_0}$

17

$$E = \frac{kq}{R^2} = \frac{9 \times 10^9 (10^{-9})}{(0.01)^2} = 90000$$

(E)

18  $U = \frac{3kq^2}{r}$

= 90

(b)

19  $U = \frac{kq_1q_2}{r}$

22  $= \frac{(9 \times 10^9)(30 \times 10^{-6})(6.5 \times 10^{-6})}{5 \times 10^{-2}} = 35.1$

≈ 35 (a)

20\*  $mg - Eq = 0$

$mg = Eq$

$E = \frac{mg}{q} \Rightarrow \frac{2k\lambda}{y} = \frac{mg}{q}$

$\lambda = \frac{mgy}{2qk} = 2.2 \times 10^{-10} \text{ C/m}$

21  $\phi = EA \cos \theta$   $\theta = 180$

$\phi = -EA = -(3.2 \times 10^3)(0.5)^2 = -80$

(d)

22  $\omega = U = Vq = 100(2) = 200$

(a)

24  $q = \epsilon_0 \phi = (8.85 \times 10^{-12})(565) = 5 \times 10^{-9} \text{ C} = 5 \text{ nC}$  (b)

25  $F_{\text{net}} = \frac{kq_1q_2}{r_{12}^2} + \frac{kq_2q_3}{r_{23}^2}$

(a) 167.2 N to right

26  $F = Eq = 400(0.02) = 8$  (a)

27  $F_1 = \frac{kq_1q_2}{r^2}$   $F_2 = \frac{k \frac{1}{4} q_1 \frac{1}{4} q_2}{\frac{r}{2}^2} = \frac{1}{4} F_1$  (c)

28  $V = \frac{E}{R} = \frac{2000}{5 \times 10^{-2}} = 4 \times 10^4$  (d)

29  $q = \rho V = 6.1 \times 10^{-4} \left[ \frac{4}{3} \pi (4.5 \times 10^{-2})^3 - \frac{4}{3} \pi (3.7 \times 10^{-2})^3 \right]$

~~$(6.1 \times 10^{-4}) \left[ \frac{4}{3} \pi (0.8 \times 10^{-2})^3 \right] = 1.309 \times 10^{-6}$~~

$(6.1 \times 10^{-4}) \left[ \frac{4}{3} \pi (4.5 \times 10^{-2})^3 - \frac{4}{3} \pi (3.7 \times 10^{-2})^3 \right] = 1.03 \times 10^{-7} \approx 1 \times 10^{-7}$  (a)